



THE EFFICIENCY OF VARIOUS
COMPUTERS AND OPTIMIZATIONS
IN PERFORMING FINITE
ELEMENT COMPUTATIONS

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METHODS FOR COMPUTATIONAL EFFICIENCY

COMPILER OPTIMIZATION

MULTIPLE PROCESSORS

WELL CHOSEN COMPUTER
FAST
CHEAP



COMPILER OPTIMIZATION

FORTRAN

OPTIMIZATION	SPEED
O0 (DEBUG)	1
O1 (DEFAULT)	
O2	1.62
O3 (AGGRESSIVE)	1.64



COMPILER OPTIMIZATION

SGI SPECIFIC

PIPELINE (WHEN 4
OPERATIONS CAN BE DONE
SIMULTANEOUSLY)

SPEEDUP: 1.8



MULTIPLE PROCESSORS

THREADING

MPI PARALLELIZATION

MULTIPLE JOBS



How Much Can a Program Speed Up?

Parallel Speedup $X = t_1/t_N$

X: parallel speedup
 t1: time for the best nonparallel execution
 tN: time for the parallel version on N cpus

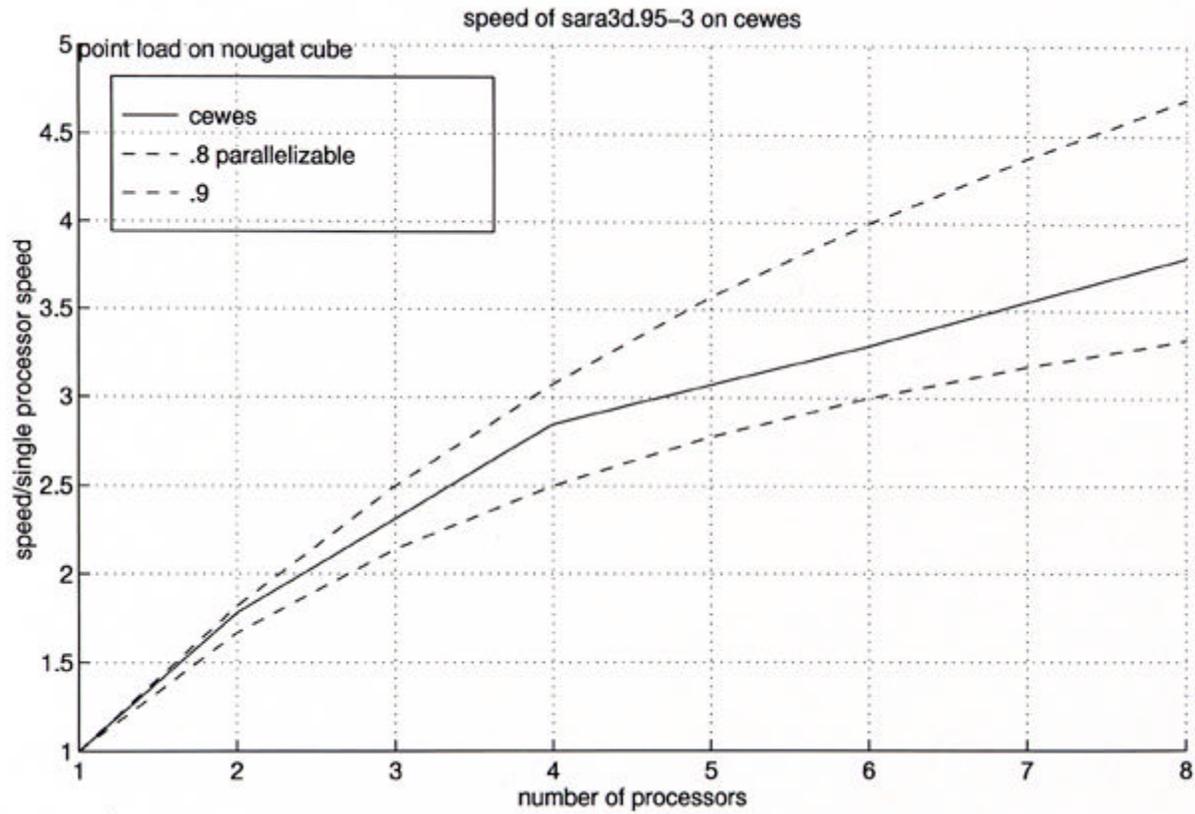
Ideal speedup $X_{ideal} = N$

Amdahl's Law $X_A = \frac{s+p}{s+p/N} = \frac{1}{s+p/N} < \frac{1}{s}$

X_A: max sustainable speedup
 p: parallelizable portion of the program
 s: non-parallelizable portion (s+p=1)
 N: number of CPUs used.

Max sustainable speedup on N CPUs with p% parallelism

p \ N	2	4	8	16	32	64
50%	1.33	1.60	1.78	1.9	1.9	2.0
75%	1.60	2.29	2.91	3.4	3.7	3.8
90%	1.82	3.08	4.71	6.4	7.8	8.8
95%	1.90	3.48	5.93	9.1	12.5	15.4
99%	1.98	3.88	7.48	13.9	24.4	39.3





THREADING

REQUIRES LARGE VECTOR TO BE PROCESSED

SPEED OF SARA3D WITH BW = 1116 ON SGI R10000 POWER CHALLENGE

PROCESSORS	SPEED	SPEED/PROC
1	1	1
4	2.2	0.55
8	1.9	0.238



MPI PARALLELIZATION

SEND JOBS TO PROCESSORS FROM
WITHIN CODE

MUST LEARN MPI

ONE PROCESSOR MUST BABY SIT
OTHERS

PROCESSORS MUST WAIT FOR
EACH OTHER

MORE EFFICIENT THAN THREADING
WHEN USING MANY PROCESSORS

NEEDS RAM AND DISK SPACE FOR
EACH JOB



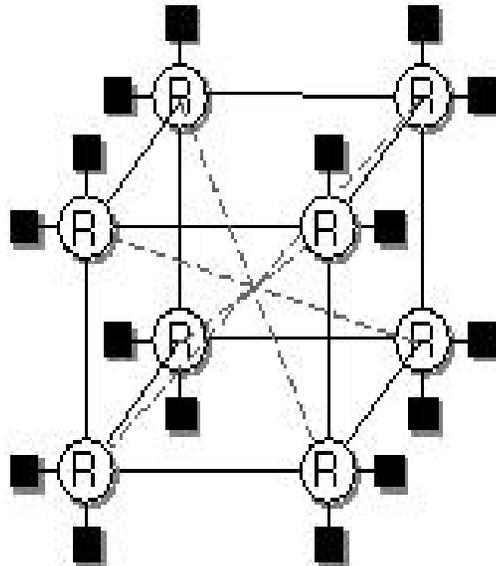
MPI PARALLELIZATION

SPEED ON SGI R10000 ORIGIN

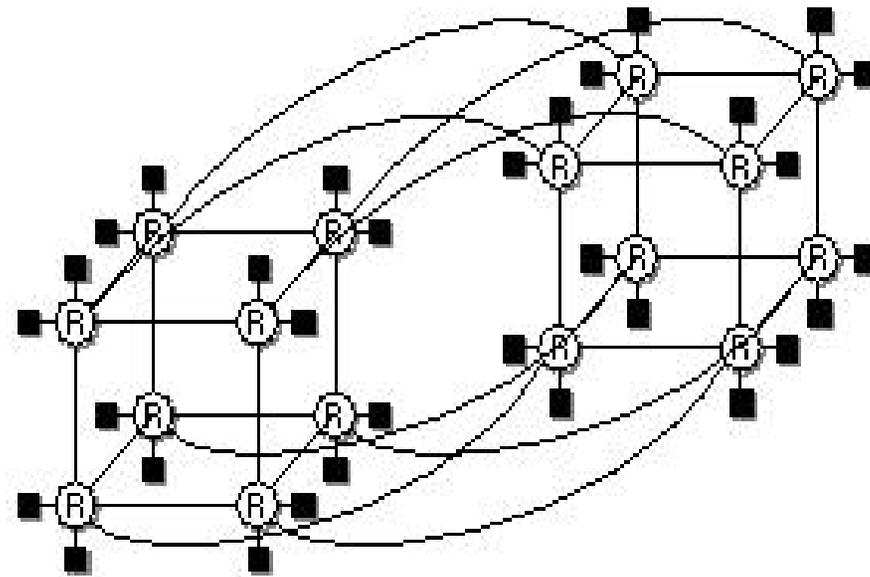
PROCESSORS	SPEED	SPEED/PROC
1	1	1
2	0.75	0.375
5	2.1	0.42
40	15.5	0.39

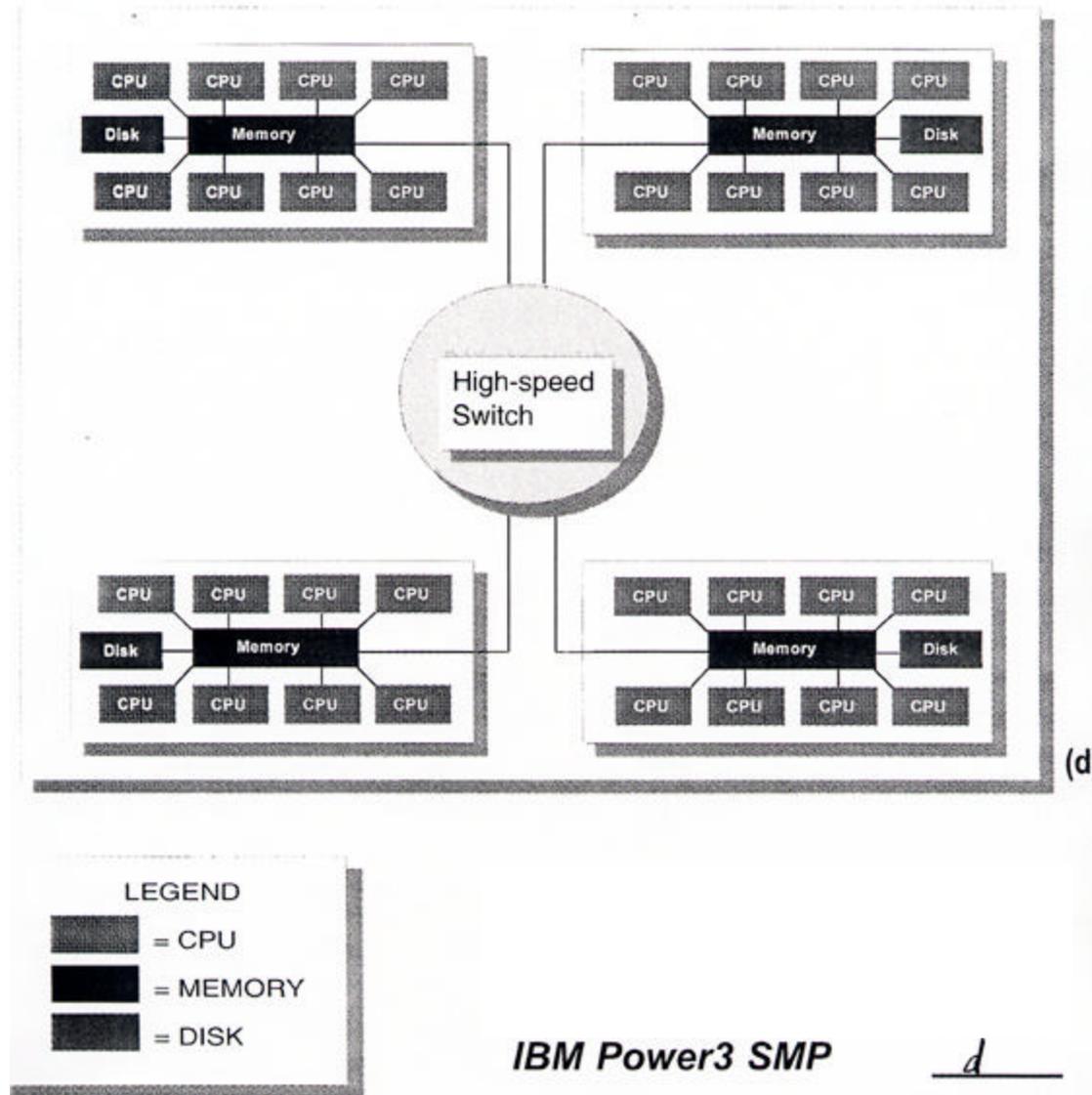


32 Processor System



64 Processor System





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12



MPI AND THREADING

IBM SMP

NODES	MPI JOBS/NODE	THREADS/MPI JOB	SPEED	SPEED/PROC
1*	1	8	8	1
1	2	4	6.0	0.75
1	4	2	4.7	0.58
2	1	8	8.8	0.55
2	4	2	4.9	0.31
13	2	4	29.1	0.28

***NO MPI**



COST OF HAVING MULTIPLE PROCESSORS

SGI ORIGIN

PROCESSORS	CAPACITY	COST (1996)	COST/PROC
4	4	\$41K	\$10K
4	8	\$85K	\$21K
8	8	\$175K	\$22K
8	128	\$271K	\$34K
128	128	\$4116K	\$32K



Computer comparison

	speed/PROC (SPECFP95)	cost/PROC	cost/speed
SGI origin	23.7	\$32,000	1350
IBM SMP	48.8	\$27,000	544
Compaq alpha	48.1	\$13,500	281



COMPUTER USING PARALLELIZATION

	Efficiency	Adjusted speed/proc	Cost/speed
SGI origin	0.39	9.2	3462
IBM SMP	0.28	13.7	1944
Compaq alpha	1	48.1	281



CONCLUSIONS

OPTIMIZE YOUR CODE WHEN
COMPILING

THREADING SPEEDS UP
CALCULATION WITHOUT TAKING
MORE RAM OR DISK

MPI PARALLELIZATION IS ALWAYS
LESS EFFICIENT THAN SPLITTING
UP JOB

COST OF COMPUTERS ALLOWING
HIGH PROCESSOR
COMMUNICATION IS PROHIBITIVE

BEST CHOICE IS SEVERAL SMALL
WORKSTATIONS